

# 3 Linear Models I

Note Title

9/7/2011

Today: Quiz  
Homework

Multiple Comparisons

Extending R

- agricolae package

- RFS package

} on R  
script

\* Linear models

## Multiple comparisons

In our ANOVA-type tests, we merely were able to conclude that (at least) one population had a different mean.

How boring! (so what?)

It is much more interesting to ask "which?"

Solution: Multiple t-tests

Problem: inflated Type I Error rates

Solution: Bonferroni

Problem: Far too conservative,

Solution: Use different tests

Options: • Fisher's LSD test

• Tukey's HSD test

• the Student-Newman-Keuls test

• Kruskal's test

• Many others

Which to use?

If you used ANOVA, use HSD

If you used Kruskal-Wallis, use Kruskal

How? In R, library agricolae  
then use `HSD.test(mmt, grp, df1, df2)`  
or `kruskal(mmt, grp)`

Both will output labels that separate the groups into distinct classes

ex

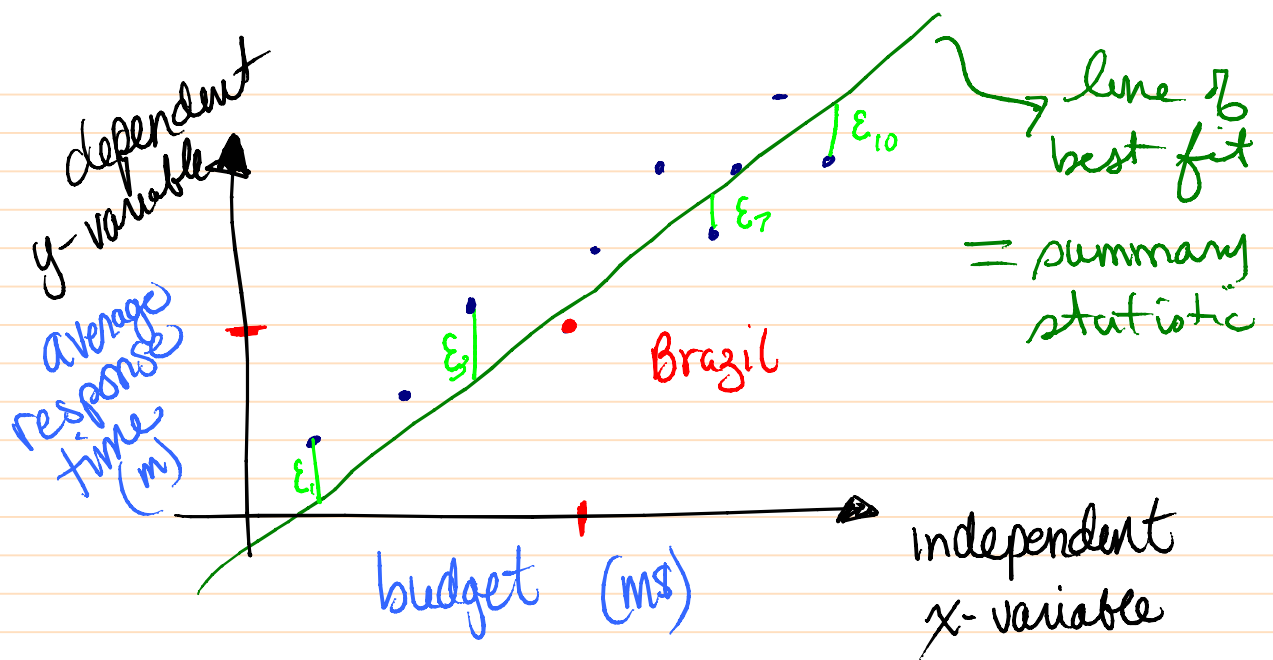
A	doves	- lone group
B	wrens	- lone group
C	geese	} statistically similar
C	ducks	

## Linear Models

Thus far: dep var = continuous  
ind dep var = discrete

Next: dep var = continuous  
ind var = continuous

Usually plotted on a scatterplot ↴



With assumptions, the line of best fit becomes a regression line



Assumptions: 1. Independent variables ARE independent  
2.  $\varepsilon \sim N(0, \sigma^2)$

These assumptions are needed to draw conclusions on the population using our sample of data.

In R, the function to do linear modeling is `lm`:

$$\text{lm}(\text{deprvar} \sim \text{indepvar}_1 + \text{indepvar}_2 + \dots)$$

the prediction equation is

$$\text{deprvar} = \hat{\beta}_0 + \hat{\beta}_1 \text{indep}_1 + \hat{\beta}_2 \text{indep}_2 + \dots$$

this is an additive model

$\Rightarrow$  effects are independent  
of each other

If we believe the effects are NOT indep,  
we use an *interaction* model

$$\downarrow$$
$$\text{lm}(\text{depress} \sim \text{indep}_1 * \text{indep}_2 + \text{indep}_3)$$

ex:  $\text{lm}(\text{happy} \sim \text{income} * \text{male})$

This means:  $\underbrace{\text{income effect}}_{\text{differs for the different genders}}$

## Testing assumptions

1. Indep vars are independent  
Correlation table & Correlation tests of the independent vars.

`cor(data)`

`worany(RFS)`

2.  $\epsilon \sim N(0, \sigma^2)$

1. residuals =  $\epsilon$

$\mu=0$  : `mean(resids)`

Normally : `shapiro.test(resids)`

$\sigma^2$  constant : `cor(resid, dep)`

`cor.test(resid, dep)`

residual plot:

`plot(resid ~ dep)`

`plot(model)`