

1 Tests for central tendency

Note Title

8/23/2011

This week: tests of 1 or 2 means
population vs. data discussion

ex population (theory) has a mean of μ_0
our data, however, has a mean of \bar{X}

Usually, we see $\mu_0 \neq \bar{X}$. So, do we
conclude our hypothesis is wrong? Not always

- In order to answer this, we need to know the distribution of \bar{X} if the theory is correct. That is, if the population mean is μ_0 ,

We make an

Assumption:

$$X \sim N(\mu, \sigma^2)$$

↑
is distributed as

Normal distribution
variance
expected value

For now let us pretend we know σ^2

Thm 2.1

If $X \sim N(\mu, \sigma^2)$ then $\bar{X} \sim N\left(\mu, \frac{\sigma^2}{n}\right)$

our test statistic

$$Z := \frac{\bar{X} - \mu_0}{\sqrt{\sigma^2/n}} \sim N(0, 1)$$

just standardization

The t-statistic

$$T := \frac{\bar{X} - \mu_0}{\sqrt{s^2/n}} \sim t \left(\text{df} = n-1 \right)$$

Note this difference

↑
"degrees of freedom"
the t-dist's parameter

Paired data = Repeated measurements

data looks like this

ID	mmt 1	mmt 2	diff
1	9	10	1
2	10	21	11
3	4	1	-3
5	16	12	-4

? Does mmt have an effect?

Assume Normality & equal variances.

Two samples INDEPENDENT

§2.4

1. If samples come from populations with equal variance, we perform an "equal variance" test.

§2.5

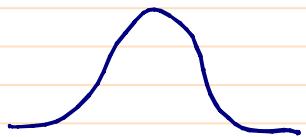
2. Otherwise, we perform the "unequal variance" test.

Assumption: Mnts Normally distributed

What if mnts not dist Normally? (App. B)

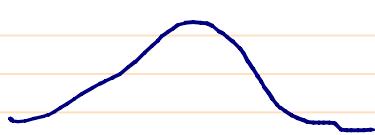
You need a "large enough" sample size.

How large? It depends on X's distribution:



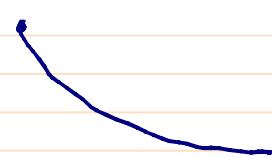
"Normal"

$n=2$



"Cauchy"

$n=30$



"Exponential"

$n=500$

Next Week:

- ANOVA
- Tests when n is too small.